

Write the answer to each of the 6 questions on a separate sheet. Please put your name and study number on each sheet. Total 100 points

**Question 1 (20 pts)**

A semiconductor has a bandgap  $E_g$ , and an effective density of states for electrons  $N_c$  and for holes  $N_v$ . The temperature is  $T$ . A PN junction is formed by doping the semiconductor with a donor density  $N_D$  and an acceptor density  $N_A$ . The semiconductor is in the extrinsic regime.

- Give an expression for the position of the Fermi energies in the (bulk) P and N doped regions. (3 pts)
- Draw and explain the band structure of a PN junction. Describe why depletion regions are formed. Give the expression for the widths of the depletion regions in the P and N regions. (3 pts)
- Give an expression for the built-in potential. (2 pts)
- Describe how/if the band diagram changes for equilibrium, forward and reverse directions. Make drawings. (3 pts)
- The width of the depletion region changes when a bias voltage is applied. Does that change the operation of the PN diode? Give arguments why/ or why not it changes the operation of the diode. (2 pts)
- Give the expression for the I/V characteristics of a PN junction. (2 pts)
- Describe a few mechanisms which can lead to non-ideal behavior of the PN junction. (2 pts)
- Draw the band diagram for a Schottky junction for equilibrium, forward and reverse directions. (3 pts)

**Question 2 (10 pts)**

Consider a metal-insulator-semiconductor (MIS) junction. The semiconductor is N-doped.

- Give the band diagram for the following regimes: 1) flatband condition, 2) depletion regime, 3) inversion regime, 4) accumulation regime. Describe where the mobile carriers are, and what type they are (electrons/holes). (5 pts)
- Give a schematic diagram of a metal-oxide-semiconductor field effect transistor. In which of the above regimes should the MOSFET be operated? (5 pts)

**Question 3 (10 pts)**

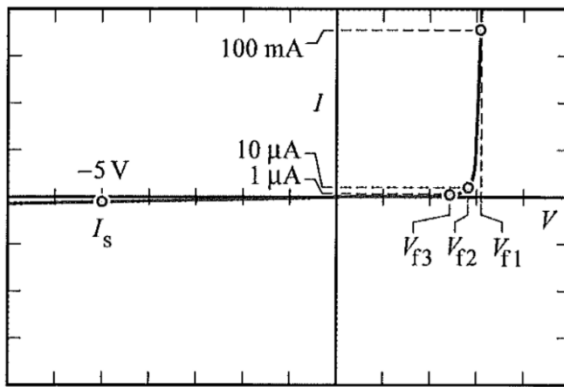
- Describe the operation of a single electron transistor (SET). Give a schematic diagram of a single electron transistor. Show the distribution of the charges when the current through the transistor is off, and when it is on. (5 pts)
- Discuss what is needed for a good operation of the transistor. Consider the role of capacitance, temperature, resistance and possible other effects which can influence the operation. (3 pts)
- Do you think that single electron transistors can replace conventional field effect transistors? Give some reasons why, or why not. (2 pts)

**Question 4 (total 20 pts)**

Consider a light-emitting diode based on an inorganic semiconductor. The LED emits light at a wavelength of 620 nm.

- a) What is the relation between the band gap of the semiconductor and the energy of the emitted light? Explain your answer. (5 pts)
- b) Calculate the luminous efficiency assuming that the LED has an external quantum efficiency of 50%. (5 pts)
- c) Real (i.e. non-ideal) LEDs have finite series and shunt resistances. Usually, the current-voltage characteristic of an LED is characterised by four critical points (see graph):

- forward voltage 1:  $V_{f1}$  (at operating current, 100 mA)
- forward voltage 2:  $V_{f2}$  (small forward current, 10  $\mu\text{A}$ )
- forward voltage 3:  $V_{f3}$  (very small forward current, 1  $\mu\text{A}$ )
- reverse saturation current  $I_s$  (at -5V)



Explain the relevance of these critical points when comparing two LEDs made of the same semiconductor. (6 pts)

- d) Two GaIn LEDs have the following data:

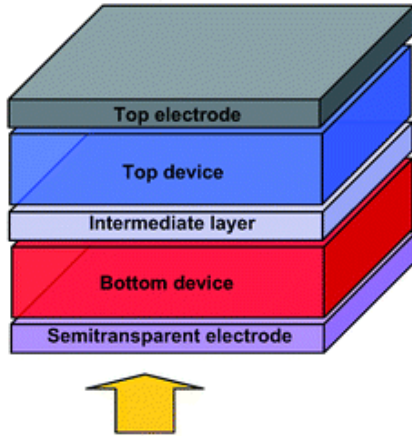
	device 1	device 2
$V_{f1}$	3.2 V	3.4 V
$V_{f2}$	2.5 V	2.0 V
$V_{f3}$	2.3 V	1.8 V
$I_s$	0.8 $\mu\text{A}$	0.8 $\mu\text{A}$

Compare these 2 devices; which one has the more desirable properties?

Explain your answer. (4 pts)

**Question 5 (total 20 pts)**

- a) Explain why even an ideal solar cell cannot have an efficiency of 100% (5 pts).
- b) What is the optimal band gap for a solar cell? (2 pts)
- c) Two semiconductors with different band gaps can be combined to make a tandem solar cell (see image below). Light that is not absorbed by the bottom cell may then be absorbed by the top cell. The efficiency of such a tandem cell can exceed the Shockley-Queisser limit. Why? (6 pts)



- d) What is the crucial difference between organic semiconductors and the classical inorganic semiconductors that are being used for PV, under illumination? (3 pts)
- e) A typical silicon pn junction solar cell consists of a thick base (p-doped) and a thin emitter (n-doped). The open-circuit voltage of such a pn junction is limited by the diffusion voltage. How is the diffusion voltage related to the doping levels of the base and emitter? Why is it better to combine a highly doped emitter with a moderately doped base instead of vice versa? (4 pts)

**Question 6 (20 pts)**

Consider a GMR device (Ferromagnet/Spacer/Ferromagnet) where the thickness of two identical ferromagnets is given by  $t_F$ , the resistivity of spin-up and spin-down electrons is given by  $\rho_M$  and  $\rho_m$  respectively and  $t_s$  and  $\rho_s$  represent the thickness and resistivity of the spacer layer.

- a) Using the parallel-resistor model write down the expression for the resistance of the device in both parallel and antiparallel configuration (NOT the GMR ratio).(6 pts)
- b) What are the two common device configurations (device geometries) used for measuring a GMR device? (2 pts)
- c) Give a key difference between electrical conduction in a ferromagnetic material (such as Co) and a metal (such as Cu). (2 pts)
- d) Draw and describe a Magnetic Tunnel Junction device (MTJ). (2 pts)
- e) Write down the expression for Spin polarization of typical ferromagnets at  $E_F$ . (1 pt)
- f) Express Tunnel Magnetoresistance (TMR) in terms of spin-polarization ( $P_1, P_2$ ) of the ferromagnets. (2 pts)
- g) What are the most important (write down at least 2) requirements for spin-dependent tunnelling to occur in such MTJ's. (2 pts)
- h) Write down the expression for tunnelling spin polarization (TSP)- how does TSP differ from spin polarization. (2 pts)